

# Biometric Liveness Detection Based on Cross Modal Fusion

Girija Chetty

National Center for Biometric Studies  
Faculty of Information Science and Engineering  
University of Canberra  
Girija.chetty@canberra.edu.au

**Abstract** - *In this paper we propose liveness checking technique for multimodal biometric authentication systems based on audio-visual cross-modal fusion. Liveness checking ensures that biometric cues are acquired from a live person who is actually present at the time of capture for authenticating the identity. The liveness check based on mutual dependency models is performed by fusion of acoustic and visual speech features which measure the degree of synchrony between the lips and the voice extracted from speaking face video sequences. Performance evaluation in terms of DET (Detector Error Tradeoff) curves and EERs (Equal Error Rates) on publicly available audiovisual speech databases show a significant improvement in performance of proposed fusion of face-voice features based on mutual dependency models.*

**Key Words:** multimodal, face-voice, speaker verification, cross modal fusion.

## 1 Introduction

Most of the commercial biometric identity authentication systems currently deployed are based on modeling the identity of a person based on unimodal information, i.e. face, voice, or fingerprint features. Also, many current interactive civilian human computer interaction applications are based on speech based voice features, which achieve significantly lower performance for operating environments with low signal-to-noise ratios (SNR). For a long time, use of acoustic information alone has been a great success for several automatic speech processing applications such as automatic speech transcription or speaker authentication, while face identification systems based visual information alone from faces also proved to be of equally successful. However, in adverse operating environments, performance of either of these systems could be suboptimal. Use of both visual and audio information can lead to better robustness, as they can provide complementary secondary clues that can help in the analysis of the primary biometric signals [1]. In

extreme cases, primary biometric (visual or acoustic) information can even be used on its own. For instance, it is well known that deaf people can learn how to lip read. The joint analysis of acoustic and visual speech improves the robustness of automatic speech recognition systems [2, 3].

There have been several systems proposed on use of joint face-voice information for improving the performance of identity authentication systems. However, most of these state-of-the-art approaches are based on independently processing the voice and face information and then fusing the scores – score fusion [4,5,6]. A major weakness of these systems is that they do not take into account fraudulent replay attack scenarios into consideration, leaving them vulnerable to spoofing by recording the voice of the target in advance and replaying it in front of the microphone, or simply placing a still picture of the target's face in front of the camera. This problem can be addressed with liveness checking, which ensures that biometric cues are acquired from a live person who is actually present at the time of capture for authenticating the identity. With the diffusion of Internet based authentication systems for day-to-day civilian scenarios at a astronomical pace [7], it is high time to think about the vulnerability of traditional biometric authentication approaches and consider inclusion of liveness checks. Though there is some work in fingerprint based liveness detection techniques [8,9], there is hardly any work in liveness checks based on user-friendly biometric identifiers (face and voice), which enjoy more acceptability for civilian access control scenarios.

A significant progress however, has been made in independent processing of face only or voice only based authentication approaches [1,2,3,4,5,6], without taking into consideration an inherent coupling that exists between jointly occurring some primary biometric identifiers. Some preliminary approaches (such as the one described in [7, 8] address liveness checking problem by jointly modeling the acoustic and visual speech features for testing liveness. They involve the fusion of acoustic, appearance and shape based lip features for jointly modeling the co-occurring face-voice dynamics in

speaking face video sequences. The method introduced in [7] fuses the speech and lip parameters in a single audiovisual feature vector stream, and then used to model each client within a Gaussian mixture model (GMM). The results obtained with this method were impressive (1% equal error rate). However, easy replay attacks were considered - a voice recording and a still photograph, and no tests for more complex replay attacks were shown. Another method described in [8] uses co-inertia analysis (CoIA) based on correlation evolution to create liveness scores based on different delays between audio and image sequences.

In this paper we propose a novel Bayesian fusion approach based on mutual dependency models for joint analysis of acoustic and visual speech features for incorporating liveness information in the authentication paradigm. The rest of the paper is organized as follows. Section 2 describes the motivation for using mutual dependency models, and the proposed liveness check approach is described in Section 3. Section 4 details the data corpora used and the experimental evaluation of the proposed mutual dependency models and Bayesian fusion approach, with Section 5 summarizing the conclusions drawn from this work and plans for further research.

## 2 Motivation for Cross-modal Fusion

The motivation to use cross-modal fusion models is based on the following two observations: The first observation is in relation to any video event, for example a speaking face video, where the content usually consists of the co-occurring audio and the visual elements. Both the elements carry their contribution to the highest level semantics, and the presence of one has usually a “priming” effect on the other: when hearing a dog barking we expect the image of a dog, seeing a talking face we expect the presence of her voice, images of a waterfall usually bring the sound of running water etc. A series of psychological experiments on the mutually dependent cross-modal influences [9, 10] have proved the importance of synergistic fusion of the multiple modalities in the human perception system. A typical example of this kind is the well-known McGurk effect [9]. Several independent studies by cognitive psychologists suggest that the type of multi-sensory interaction between acoustic and orafacial articulators occurring in the McGurk effect involves both the early and late stages of integration processing [9,10]. It is likely that a human brain uses a hybrid form of fusion that depends on the availability and quality of different sensory cues.

Yet, in audiovisual speech and speaker verification systems, the analysis is usually performed separately on different modalities, and the results are brought together using different fusion methods. However, in this process of separation of modalities, we lose valuable cross-modal information about the whole event or the object we are trying to analyze and detect. There is an inherent

association between the two modalities and the analysis should take advantage of the synchronised appearance of the relationship between the audio and the visual signal. The second observation relates to different types of fusion techniques used for joint processing of audiovisual speech signals. The late-fusion strategy, which comprises decision or the score fusion, is effective especially in case the contributing modalities are uncorrelated and thus the resulting partial decisions are statistically independent. Feature level fusion techniques, on the other hand, can be favoured (only) if a couple of modalities are highly correlated. However, jointly occurring face and voice dynamics in speaking face video sequences, is neither highly correlated (mutually dependent) nor loosely correlated nor totally independent (mutually independent). A complex and nonlinear spatiotemporal coupling consisting of highly coupled, loosely coupled and mutually independent components may exist between co-occurring acoustic and visual speech signals in speaking face video sequences [11, 12]. The compelling and extensive findings by authors in [11] validate such complex relationship between external face movements, tongue movements, and speech acoustics when tested for consonant vowel (CV) syllables and sentences spoken by male and female talkers with different visual intelligibility ratings. They proved that there is a higher correlation between speech and lip motion for C/a/ syllables than for C/i/ and C/u/ syllables. Further, the degree of correlation differs across different places of articulation, where lingual places have higher correlation than bilabial and glottal places. Also, mutual coupling can vary from talker to talker; depending on the gender of the talker, vowel context, place of articulation, voicing, and manner of articulation and the size of the face. Their findings also suggest that male speakers show higher correlations than female speakers. Further, the authors in [12] also validate the complex, spatiotemporal and non-linear nature of the coupling between the vocal-tract and the facial articulators during speech production, governed by human physiology and language-specific phonetics. They also state that most likely connection between the tongue and the face is indirectly by way of the jaw. Other than the biomechanical coupling, another source of coupling is the control strategy between the tongue and cheeks. For example, when the vocal tract is shortened the tongue does not get retracted.

Due to such a complex nonlinear spatiotemporal coupling between speech and lip motion, this could form a good candidate for detecting liveness, and modelling the speaking faces by capturing this information can make the biometric authentication systems less vulnerable to spoof and fraudulent replay attacks, as it would be almost impossible to spoof a system which can accurately distinguish the artificially manufactured or synthesized speaking face video sequences from the live video sequences. We propose a Bayesian fusion approach based

on mutual dependency modelling to address this problem. Next section briefly describes the proposed approach.

### 3 Cross Modal Fusion Models

Cross Modal Fusion models based on Canonical Correlation Analysis (CCA), first proposed by Hotelling [13], is a method of determining a linear space where the correlations between two sets of variables are maximized. This approach has been successfully applied to sets of variables that are manifestations of a set of hidden variables, examples of this are fMRI and image retrieval[14]. There is an obviously similarity with audio-visual speaking face modelling since the motions of articulators and the speech produced are fundamentally linked. However, CCA is derived as a linear process and this limitation becomes apparent in the cases where the underlying relationship is non-linear [15], such as the complex nonlinear spatiotemporal correlations between the speech and lip-motion in speaking face video sequences. To circumvent this linearity constriction the “kernel trick” can be employed, replacing an inner product by a projection of the data into a higher dimensional space, and performing CCA in this realized dual representation [15].

We present a novel approach to extract the nonlinear correlations between audio-lip motion articulators in this paper by performing kernel Canonical Correlation Analysis (kCCA) on Mel Frequency Cepstral Coefficients (MFCC) voice features and the lip motion features extracted from a biological inspired optical flow algorithm called Multi Channel Gradient Model (MCGM).

The MCGM is a neurophysiological and psychophysical inspired unified motion algorithm [15]. MCGM functions by modeling the behaviors of V1/V2 cells and evaluates the ratio of temporal and spatial gradients to establish local velocity estimates. From one sequence of lip region images it is possible to derive two sets of visual information from MCGM, initially a sequential series of frames are parsed by MCGM algorithm, calculating the relative motions between successive frames. Additionally, a current frame of data is processed against a fixed open mouth frame, calculating the absolute motions of the mouth. MCGM processing results in a matrices of equal size to the input frames, each containing speed and angular information for a given pixel. Applying (linear) Principal Component Analysis (PCA) produces a linear space onto which the motions can be mapped, reducing the dimensionality of the visual features.

Mel-Frequency Cepstral Coefficients (MFCC) are classical acoustic speech features used in automatic speech processing [16]. They are state-of-the-art features in many applications, including automatic speech recognition and speaker verification systems. For obtaining a MFCC feature vector, the voice signal is transformed into the frequency domain via windowed Fast Fourier Transform and then mapped on to the Mel scale, a human perceptual

scale of frequency [16]. A (logarithmically spaced) filter bank is constructed over this Mel frequency spectrum, and from this the logarithm of the power spectrum is determined. A discrete time cosine transform is performed over the power spectrum and the MFCCs are calculated. Most of the information about human voice from speech can be captured by retaining 10-12 most significant MFCC features, the first-order time-derivatives(delta features), the pitch and the signal energy.

To account for the lack of synchronization between speech features and lip motion features, rate interpolation can be done by up sampling the MCGM features to obtain the synchronized MCGM-MFCC features. Once the acoustic MFCC features and MCGM lip motion features are obtained, kCCA is implemented by first mapping them onto the kernel space using polynomial kernels and then performing CCA. Since, the kCCA involves, implementing CCA in a higher dimensional nonlinear space, it has the capability to capture and track the nonlinear correlations between different features. Parameter tuning for kCCA can be performed offline on an independent data set.

For extracting the mutually independent components of the audio and visual signals, another powerful statistical technique called independent component analysis (ICA) is performed, which treats the observed variables as a mixture of independent sources. Two different architectures are used for Independent Component Analysis, ICA1 and ICA2 [17, 18]. In ICA1, the basis images are independent, whereas in ICA2 the mixing coefficients are independent. We utilize the ICA2 architecture, where each pixel for lip images are considered as a mixture of independent coefficients. If  $X$  is a data matrix incorporating the measured variables, then it can be split as:  $X = AS$  where  $A$  is the mixing matrix and  $S$  contains the independent coefficients. The columns of  $A$  form a basis for the database and the columns of  $S$  provide ICA-features for the corresponding lip images residing in the columns of the data matrix  $X$ .

For each pixel, all  $x$  and  $y$  coordinates of a lip image are concatenated to a single vector. Its dimensionality is then reduced by applying PCA to the training set of  $x$ - $y$  co-ordinate vectors. Each face is then represented by the first  $K$  PCA coefficients. The columns of the data matrix  $X$  for the ICA analysis are constituted of PCA coefficient vectors. Then, the Fast ICA algorithm described by [17, 18] is applied to obtain the basis  $A$  and the independent coefficients  $S$ . The Bayesian fusion technique used to combine various features is described in the next section.

### 4 Multimodal Fusion

First, we derive the algorithm for performing the Bayesian fusion for liveness checks using multiple features described in the previous Section. Let us denoted the projection of audio and lip features in each of the closely coupled (kCCA), and mutually independent (ICA)

subspaces as  $f_{kCCA}$  and  $f_{ICA}$ . We also include the projection of visual information in the PCA subspace as Eigenlip features  $f_{PCA}$  [xx] as the static spatial information in face images contains identity specific information. In Bayesian framework, the most generic way of performing the fusion is to compute the joint scores expressed as a weighted summation [19, 20]:

$$\rho(\lambda_r) = \sum_{n=1}^N w_n \log P(f_n | \lambda_r) \quad \text{for } r=1,2,\dots,R \quad (1)$$

where  $\rho_n(\lambda_r)$  is the logarithm of the class-conditional probability,  $P(f_n | \lambda_r)$ , for the  $n^{th}$  modality  $f_n$  given class  $\lambda_r$ , and  $w_n$  denotes the weighting coefficient for modality  $n$ , such that  $\sum_n w_n = 1$ . Here  $f_n$  could be  $f_{kCCA}$ ,  $f_{ICA}$  or  $f_{PCA}$  features. Then the fusion problem reduces to a problem of finding the optimal weight coefficients for the nonlinear highly correlated components, loosely coupled  $f_{PCA}$  components and mutually independent  $f_{ICA}$  components. Though an adaptive fusion weight calculation would be ideally required, we selected the weights empirically and fused them using RWS (Reliability Weighted Summation) rule [19]. Since the statistical and the numerical range of these likelihood scores can vary from one modality to another, the likelihood scores were normalised within the (0, 1) interval before the RWS fusion process using a sigmoid and variance normalization as described in [20].

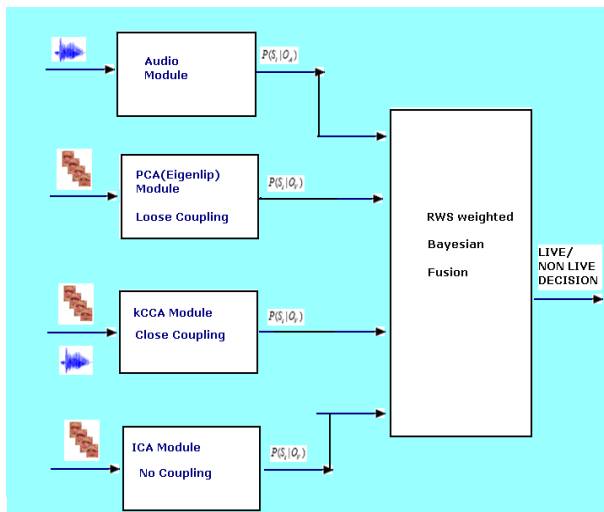


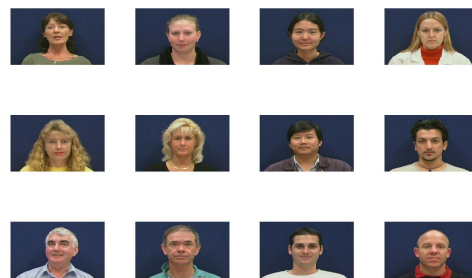
Figure 1: Block schematic of the Bayesian fusion of correlated audio-visual components

## 5 Experimental Results

Preliminary experimental results with an audio-visual speaking face video corpora VidTIMIT [21] and DaFEx [22,23] showed a significant improvement liveness

checking performance due to the detailed modelling of speaker liveness based on multiple correlation features. Figure 2 show some images from the two corpora. The details of the two corpora are given in [21], [22] and [23].

In this section, different experiments conducted to evaluate the performance of the proposed correlation features, and the Bayesian fusion of the MFCC, lip features in different subspaces PCA, kCCA and ICA liveness checking are described. The testing stage for the liveness checking scenarios is different from the tradition biometric identity verification scenarios [x.x], where the replay attack test data emulating fraudulent attacks needs to be artificially synthesised. Two different types of replay attacks were tested, one static replay attacks used in [x] and other dynamic replay attacks, where artificial speaking face sequences are synthesised from still photo, few key frames from the video sequences, lip-synched with pre-recorded speech signals.



VidTIMIT corpus images



(b) DaFeX corpus images

Figure 2: Face Images from VidTIMIT and DaFex Corpus

Liveness checking experiments involved two phases, the training phase and testing phase. In the training phase a 10-mixture Gaussian mixture model  $\lambda$  of a client's audiovisual feature vectors was built, reflecting the probability densities for the combined phonemes and visemes (lip shapes) in the audiovisual feature space. In the testing phase, the clients' live test recordings were first evaluated against the client's model  $\lambda$  by determining the

log likelihoods  $\log p(X|\lambda)$  of the time sequences  $X$  of audiovisual feature vectors under the usual assumption of statistical independence of successive feature vectors.

For testing static replay attacks, a number of “fake” or synthetic recordings were constructed by combining the sequence of audio feature vectors from each test utterance with ONE visual feature vector chosen from the sequence of visual feature vectors and keeping that visual feature vector constant throughout the utterance. Such a synthetic sequence represents an attack on the authentication system, carried out by replaying an audio recording of a client’s utterance while presenting a still photograph to the camera. Four such fake audiovisual sequences were constructed from different still frames of each client test recording. Log-likelihoods  $\log p(X'|\lambda)$  were computed for the fake sequences  $X'$  of audiovisual feature vectors against the client model  $\lambda$ . In order to obtain suitable thresholds to distinguish live recordings from fake recordings, detection error trade-off (DET) curves and equal error rates (EER) were determined. For testing dynamic replay attacks artificially synthesized speaking face video sequences were used instead of actually recorded video sequences in the data corpora.

Since the liveness checking is a two-class decision task, the system can make two types of errors. The first type of error is a False Acceptance Error (FA), where an impostor (fraudulent replay attacker) is accepted. The second error is a False Rejection (FR), where a true claimant (genuine client) is rejected. Thus, the performance is measured in terms of False Acceptance Rate (FAR) and False Reject Rate (FRR), as defined as (2) :

$$FAR \% = \frac{I_A}{I_T} \times 100 \%$$

$$FRR \% = \frac{C_R}{C_T} \times 100 \%$$
(2)

where  $I_A$  is the number of impostors classified as true claimants,  $I_T$  is the total number of impostor classification tests,  $C_R$  is the number of true claimants classified as impostors, and  $C_T$  is the total number of true claimant classification tests. The implications of this is minimizing the FAR increases the FRR and vice versa, since the errors are related. The trade-off between FAR and FRR is adjusted using the threshold  $\theta$ , an experimentally determined speaker-independent global threshold from the training/enrolment data. The trade-off between FAR and FRR can be graphically represented by a Receiver Operating Characteristics (ROC) plot or a Detection Error Trade-off (DET) plot. The ROC plot is on a linear scale, while the DET plot is on a normal-deviate logarithmic scale. For DET plot, the FRR is plotted as a function of FAR. To quantify the performance into a single number, the Equal Error Rate (EER) is often used. Here the system is configured with a threshold, set to an operating point when  $FAR \% = FRR \%$ .

It must be noted that the threshold  $\theta$  can also be adjusted to obtain a desired performance on test data (data unseen by the system up to this point). Such a threshold is known as the aposteriori threshold. However, if the threshold is fixed before finding the performance, the threshold is known as the apriori threshold. The apriori threshold can be found via experimental means using training/enrolment or evaluation data, data which has also been unseen by the system up to this point, but is separate from test data.

Practically, the a priori threshold is more realistic. However, it is often difficult to find a reliable apriori threshold. The test section of a database is often divided into two sets: evaluation data and test data. If the evaluation data is not representative of the test data, then the apriori threshold will achieve significantly different results on evaluation and test data. Moreover, such a database division reduces the number of verification tests, thus decreasing the statistical significance of the results. For these reasons, many researchers prefer to use the aposteriori and interpret the performance obtained as the expected performance. Different sets of experiments were conducted to evaluate the performance of the correlation features based on mutual dependency models and hybrid fusion features in terms of DET curves and equal error rates (EER). The performance results for different audiovisual features based on mutual dependency models in terms of DET curves and EERs in Table 1 and Figure 3 and 4.

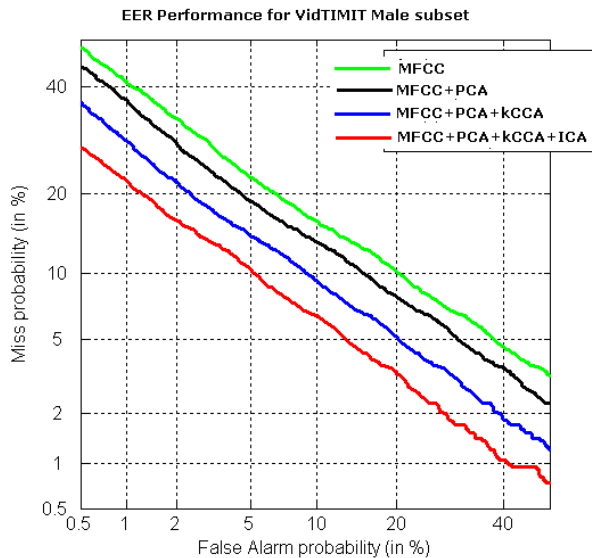


Figure 3: DET curves for audio visual features based on mutual dependency models for VidTIMIT data set

As can be seen from Table 1 and Figure 3 and 4 the results are quite promising for correlation features in kCCA space and their fusion with features in ICA and PCA space. The single mode MFCC features and PCA or Eigen lip features results in worse EERS. Further, the MGCM features on their own do not result in a good EER performance.

However, when they are fused with the kCCA projected features, they result in improved performance. Further, use of correlation features in different subspaces, PCA, ICA and kCCA result in best EERs as complete mutual dependency components (closely coupled, loosely coupled and uncoupled components are included in the modelling). Further work involves, developing an automatic fusion computation technique based on reliability scores.

Table 1: EERs for audio visual features based on mutual dependency models

Audio/ Visual Features	VidTIMIT		DaFeX	
	MALE EER (%)	FEM ALE EER (%)	MALE EER (%)	FE MALE EER (%)
$f_{mfcc}$	16.8	16.88	15.7	15.7
$f_{eigLip}$	16.2	16.2	16.64	16.64
$f_{MGCM}$	17.2	17.87	15.9	15.54
$f_{kCCA}$	14.7	15.18	14.81	15.28
$f_{ICA}$	13.03	14.12	13.12	14.4
$f_{mfcc} +$ $f_{eigLip}$	11.68	11.86	11.79	11.17
$f_{mfcc} +$ $f_{eigLip}$ $+ f_{kCCA}$	10.26	10.26	10.46	10.46
$f_{mfcc} +$ $f_{eigLip}$ $+ f_{kCCA} +$ $f_{ICA}$	8.06	8.85	9.23	9.31

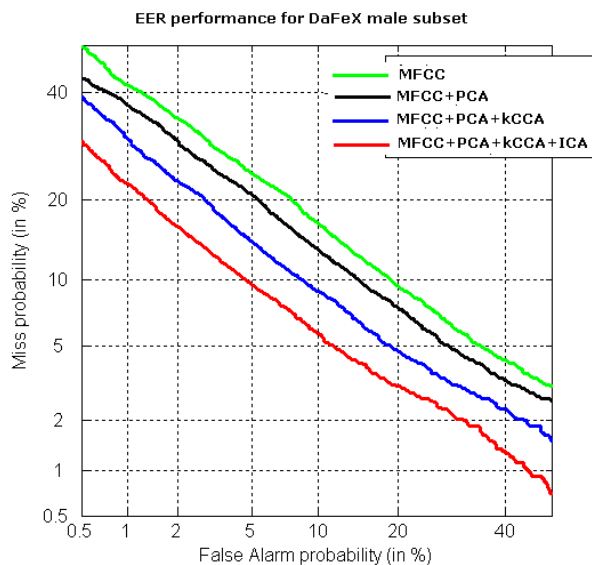


Figure 4: DET curves for audio visual features based on mutual dependency models for DaFeX data set

## 6 Conclusions

In this paper we proposed a novel method of extracting audio visual features based on mutual cross modal analysis for liveness checking in biometric identity authentication systems. Performance evaluation in terms of DET curves and EERs on VidTIMIT and DaFeX corpora, showed a significant improvement in performance of proposed features as compared to traditional single mode face or voice features.

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## 8 Appendix

Canonical Correlation Analysis CCA is a way of measuring the linear relationship between two multidimensional variables [11]. CCA searches for two sets of basis vectors related with each variable, so that the correlation of variables in new basis is diagonal and the diagonal elements are maximized. An important property of canonical correlations is that they are invariant with respect to affine transformations of the variables. This is the most important difference between CCA and ordinary

correlation analysis which highly depend on the basis in which the variables are described. A brief description of CCA technique follows.

Let two multidimensional biometric signals are represented with  $x$  and  $y$ . Further let the projection matrices be  $w_x$  and  $w_y$  such that the correlations between the projections of  $x$  and  $y$  onto  $R(w_x)$  and  $R(w_y)$

$$\rho = \frac{E[\dot{x}\dot{y}^T]}{\sqrt{E[\dot{x}\dot{x}^T]}\sqrt{E[\dot{y}\dot{y}^T]}} \quad (1)$$

where  $\dot{x} = W_x^T x$  and  $\dot{y} = W_y^T y$ . Let  $x$  and  $y$  be zero mean random variables. The total covariance matrix is defined as:

$$C = \begin{bmatrix} C_{xx} & C_{xy} \\ C_{yx} & C_{yy} \end{bmatrix} = E \begin{bmatrix} x \\ y \end{bmatrix} \begin{bmatrix} x^T & y^T \end{bmatrix} \quad (2)$$

where  $C_{xx}$  and  $C_{yy}$  are within set covariance matrices, and  $C_{xy} = C_{yx}^T$  is between-set correlation matrices. The canonical correlations between  $x$  and  $y$  can be found by solving the eigenvalue equations

$$\begin{aligned} C_{xx}^{-1} C_{xy} C_{yy}^{-1} C_{yx} w_x &= \rho^2 w_x \\ C_{yy}^{-1} C_{yx} C_{xx}^{-1} C_{xy} w_y &= \rho^2 w_y \end{aligned} \quad (3)$$

where eigenvalues  $\lambda^2$  are the squared canonical correlations and the eigenvectors  $w_x$  and  $w_y$  are normalized canonical correlation basis vectors. Only one of the eigenvalue equations needs to be solved since the solutions are related by:

$$\begin{aligned} C_{xy} w_y &= \rho \lambda_x C_{xx} w_x \\ C_{yx} w_x &= \rho \lambda_y C_{yy} w_y \end{aligned} \quad (4)$$

where

$$\lambda_x = \lambda_y^{-1} = \sqrt{\frac{w_y^T C_{yy} w_y}{w_x^T C_{xx} w_x}} \quad (5)$$